| FACULTY OF HEALTH AND | ПATIIBIA UMIVERSITY | APPLIED SCIENCES |
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| DEPARTMENT OF | OF SCIEПCE AחD TECHMOLOGY | ACCOUNTING, |
|  | ECONOMICS AND FINANCE |  |


| QUALIFICATION: BACHELOR OF ECONOMICS |  |  |
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| QUALIFICATION CODE: 07BECO |  | LEVEL: 7 |
| COURSE CODE: ECM712s |  | COURSE NAME: ECONOMETRICS |
| SESSION: June 2022 |  | PAPER: THEORY |
| DURATION: 3 HOURS |  | MARKS: 100 |
| SECOND OPPORTUNITY EXAMINATION QUESTION PAPER |  |  |
| EXAMINER(S) | MR. PINEHAS NANGULA |  |
| MODERATOR: | Dr R. KAMATI |  |
| INSTRUCTIONS |  |  |
| 1. Answer $A L L$ the questions in section $A$ and $B$ <br> 2. Write clearly and neatly. <br> 3. Number the answers clearly. |  |  |

## PERMISSIBLE MATERIALS

1. Scientific calculator
2. Pen and Pencil
3. Ruler

## MULTIPLE CHOICE QUESTIONS

1. OLS stands for what in Econometrics?
a) Optimally Linearized Solution
b) There is no such thing in Econometrics
c) The only rock band that Econometricians are crazy about
d) Ordinary Least Squares
2. Data collected at a point in time is called
a) Cross-sectional data
b) Time series data
c) Pooled data
d) Panel data
3. Data collected for a variable over a period of time is called
a) Cross-sectional data
b) Time series data
c) Pooled data
d) Panel data
4. In the estimated model $\widehat{\log Q}_{i}=2.25-0.7 \log P_{i}+0.02 Y_{i}$, where p is the price and q is the quantity demanded of a certain good and $Y$ is disposable income, what is the meaning of the coefficient on logP?
a) If the price increases by $1 \%$, the demanded quantity will be $0.007 \%$ lower on average, ceteris paribus
b) If the price increases by $1 \%$, the demanded quantity will be $70 \%$ lower on average, ceteris paribus
c) If the price increases by $1 \%$, the demanded quantity will be $0.7 \%$ lower on average, ceteris paribus
d) None of the answers above is correct
5. In the estimated model $\widehat{\log Q}_{i}=2.25-0.7 \log P_{i}+0.02 Y_{i}$, where p is the price and q is the quantity demanded of a certain good and $Y$ is disposable income, what is the meaning of the coefficient on log $\gamma$ ?
a) If disposable income increases by a thousand dollars, the demanded quantity will be $0.02 \%$ higher on average, ceteris paribus
b) If disposable income increases by a thousand dollars, the demanded quantity will be $0.0002 \%$ higher on average, ceteris paribus
c) If disposable income increases by a thousand dollars, the demanded quantity will be $2 \%$ higher on average, ceteris paribus
d) None of the answers above is correct
6. Which of the following are alternative names for the dependent variable (usually denoted by y ) in linear regression analysis?
a) The regressand
b) The regressor
c) The explanatory variable
d) None of the above
7. Which of the following statements is TRUE concerning OLS estimation?
a) OLS minimises the sum of the vertical distances from the points to the line
b) OLS minimises the sum of the squares of the vertical distances from the points to the line
c) OLS minimises the sum of the horizontal distances from the points to the line
d) OLS minimises the sum of the squares of the horizontal distances from the points to the line.
8. The residual from a standard regression model is defined as
a) The difference between the actual value, $y$, and the mean, $y$-bar
b) The difference between the fitted value, $y$-hat, and the mean, $y$-bar
c) The difference between the actual value, $y$, and the fitted value, $y$-hat
d) The square of the difference between the fitted value, $y$-hat, and the mean, $y$-bar
9. Which one of the following statements best describes the algebraic representation of the fitted regression line?
a) $\hat{y}_{t}=\hat{\alpha}+\hat{\beta}_{z}+\hat{u}_{t}$
b) $\hat{y}_{z}=\hat{\alpha}+\hat{\beta} x_{2}$
c) $\hat{y}_{z}=\hat{\alpha}+\hat{\beta}_{x}+u_{t}$
d) $y_{t}=\hat{\alpha}+\hat{\beta_{z}}+\hat{u}_{t}$
10. Which one of the following statements best describes a Type II error?
a. It is the probability of incorrectly rejecting the null hypothesis
b. It is equivalent to the power of the test
c. It is equivalent to the size of the test
d. It is the probability of failing to reject a null hypothesis that was wrong

SECTION B
[80 MARKS]

## QUESTION ONE

All questions pertain to the simple (two-variable) linear regression model for which the population regression equation can be written in conventional notation as:
$Y_{i}=\beta_{1}+\beta_{2} X_{i}+u_{1}$ equation 1
where $Y_{i}$ and $X_{i}$ are observable variables, $\beta_{1}$ and $\beta_{2}$ are unknown (constant) regression coefficients, and $u_{i}$ is an unobservable random error term. The Ordinary Least Squares (OLS) sample regression equation corresponding to regression equation (1) is
$Y_{i}=\hat{\beta}_{1}+\hat{\beta}_{2} X_{i}+\hat{u}_{i}$ equation 2
where $\hat{\beta}_{1}$ is the OLS estimator of the intercept coefficient $\beta_{1}, \hat{\beta}_{2}$ is the OLS estimator of the slope coefficient $\beta_{2}, u_{i}$ is the OLS residual for the i -th sample observation, and N is sample size (the number of observations in the sample).
a) State the Ordinary Least Squares (OLS) estimation criterion. State the OLS normal equations.
b) Derive the OLS normal equations from the OLS estimation criterion.
c) Show that the OLS slope coefficient estimator $\hat{\beta}_{1}$, is a linear function of the $Y_{i}$, sample values.
d) Stating explicitly all required assumptions, prove that the OLS slope coefficient estimator $\hat{\beta}_{2}$ is an unbiased estimator of the slope coefficient $\beta_{2}$.

## QUESTION TWO

## [20 MARKS]

a) What do we mean by a linear regression model?
b) The following are linear intrinsically linear regression models. You are required to transform them into linear regression models
i. $\quad \ln Y_{i}=\frac{1}{1+e^{\beta_{1}+\beta_{2} x_{i}+u_{i}}}$
ii. $\quad \ln Y_{i}=\frac{1}{\beta_{1}+\beta_{2} X_{i}+u_{i}}$
iii. $\quad Y_{i}=\frac{X^{2}}{\exp \left(\beta_{1}+\beta_{2} X_{i}+u_{i}\right)}$
[4 marks]
iv. $\quad \ln Y_{i}=1+\exp \left(\beta_{1}+\beta_{2} X_{i}\right)$
[4 marks]

## QUESTION TWO

[20 MARKS]
The following is the econometric model which is presented in four different forms. You are require to interpret each of them.
a) $\hat{C}=-8.078+0.70641$ Income
b) $\hat{C}=-18.072+22.73841$ Logincome
c) $\widehat{\log C}=7.203+0.000218$ Income
d) $\widehat{\log C}=-0.2957+1.0464$ Logincome

## QUESTION FOUR

[10 MARKS]
The data in the table below refer to a total population of 40 families in a hypothetical community and their weekly income (I) and weekly consumption expenditure ( $C$ ), both in dollars. The 28 families are divided into 5 income groups (from $N \$ 200$ to $N \$ 1000$ ) and the weekly expenditures of each family in the various groups are as shown in the table below.

| Income $I_{i}$ | 200 | 400 | 600 | 800 | 1000 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Consumption | 150 | 300 | 573 | 698 | 890 |
|  | 189 | 350 | 450 | 798 | 850 |
|  | 123 | 287 | 470 | 700 | 950 |


|  | 190 | 390 | 560 | 758 | 863 |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  |  | 300 | 498 | 766 |  |
|  |  | 396 | 564 | 788 |  |
|  |  |  | 497 |  |  |
|  |  |  | 500 |  |  |

a) Calculate the conditional mean and unconditional mean value of $C_{i}$ [6 marks]
b) Use the answer in part a) to draw the population regression line or population regression curve
[4 marks]

## All the best

